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# New approach for kinetic parameters determination for hydrothermal oxidation reaction

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## Abstract

The purpose of this study is to test Runge–Kutta algorithm to obtain reliable kinetic parameters for the hydrothermal oxidation of organic compounds. A tubular reactor system was used to carry out the oxidation of several model compounds: acetic acid, methanol and phenol. All experiments were performed in isothermal conditions in a temperature range varying from 250 to 500 °C and at a constant pressure of 25 MPa. Three different methods, namely pseudo-first-order kinetics, multiple linear regression and Runge–Kutta algorithm, were used to determine the kinetic parameters. Results obtained by these different methods were similar, so that Runge–Kutta algorithm was validate for the determination of kinetic parameters. In contrast with the pseudo-first-order kinetics and the multi linear regression, Runge–Kutta algorithm was more convenient for the kinetic parameter determination starting from experiments performed at the laboratory scale or in industrial scale pilot plant facilities.

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# 1. Introduction

Oxidation of wastewaters at high pressure and temperature, so-called hydrothermal oxidation treatment (HOT), is an efficient alternative to conventional methods such as biological treatments or common chemical processes in the treatment of highly contaminated wastewaters with an organic concentration between 10 and 70 g/l [1–3]. HOT can operate in conditions below or above the critical point of water (374.2 °C and 22.1 MPa). Below the critical point of water, the process is called wet air oxidation (WAO) and it typically operates at temperatures and pressures ranging from 200 to 330 °C and from 2 to 20 MPa, respectively [4]. Above the critical point of water, the process is called supercritical water oxidation (SCWO) and it typically implies pressures and temperatures varying between 400 and 650 °C and between 25 and 35 MPa, respectively [5]. In these last conditions, the treatment of organic compounds that contain carbon, hydrogen, nitrogen and oxygen leads to the output liquid effluent and gas effluent that can be released in natural media without post-treatment [6]. Moreover, the liquid output can be used for industrial or agricultural applications.

In order to scale-up reactors for HOT of industrial wastewaters, kinetic parameters of hydrothermal oxidation reaction and heat transfer are required [7]. In the last two decades, many authors have studied kinetic parameters of hydrothermal oxidation reaction of several model compounds, like

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acetic acid, methanol and phenol. Portela et al. [8] have demonstrated, for kinetic studies on phenol, that the parameters obtained in WAO and SCWO could not be used in operating conditions different from those in which they were obtained. More generally, the kinetic parameters were relative to the reactor system in which the experimental data were obtained and were only applicable for the scale-up of a similar reactor concept. In this way, in order to predict or simulate the behaviour of industrial pilot plant facilities, extensive experimental works are needed, especially the effects of main process parameters such as temperature, and both organic and oxygen concentrations. Concerning heat transfer, this parameter was already well investigated and simulation tools are available [9,10]. The purpose of this study was to test Runge-Kutta algorithm in order to obtain reliable kinetic information for hydrothermal oxidation of organic compounds. Thus, three different approaches were tested and compared to determine the kinetic parameters for HOT of three model compounds, i.e., acetic acid, methanol and phenol.

# 2. Experimental

Fig. 1 shows a schematic diagram of the pilot plant facility developed in our laboratory [11]. This pilot plant facility was able to treat up to  $2.8 \text{ kg h}^{-1}$  aqueous wastes in a temperature range of 200-600 °C, at pressures up to 30 MPa. Main units of this equipment were connected to a data acquisition and control unit controlled by Labview software (National Instrumentation). This system permited to select, control and save main parameters as organic feed and oxygen flow rates, temperature of pre-heater and reactor and system pressure. High-pressure pump LEWA pressurized the aqueous feed solution, typically at a flow rate of 1 kg h<sup>-1</sup>. Before entering the reactor, this feed was preheated at the desired reaction temperature by an electric heater (1.5 kW) along 9 m of 316 SS tubing with an i.d. of 1.6 mm. The oxidant feed was pure oxygen pressurized by a Haskel compressor that injected the oxygen at 25 MPa, without preheating, at the input of the reactor. A mass flow meter (Brooks 5850S) allowed the selection and control of the desired flow rate in the range of  $0-100 \text{ g h}^{-1}$ . The reactor was made of Inconel 625 (36 m length and 1.6 mm i.d.). Twenty-eight thermocouples were attached to the external surface. The working reaction temperature was controlled by three external electrical heaters (1.5 kW each one) connected to a PID controller. The reactor was isolated by a calcite jacket. At the output of the reactor, the effluent was cooled by a counter current heat exchanger and afterwards, the system pressure was reduced by using a backpressure regulator. The product stream was then separated into liquid and vapor phases. For liquid samples, chemical oxygen demand (COD) was performed according to the French normalized method for water and wastewater analysis [12]. The accuracy of the COD measurements was  $\pm 5\%$ since the organic matter studied was water soluble. The initial concentration of organic compounds was  $10 \text{ g } \text{l}^{-1}$  in terms of COD. All experiments were performed in duplicate.

The experiments were carried out in isothermal conditions with temperatures ranging from 250 to 500 °C and at a constant pressure of 25 MPa. In the case of phenol, since it was easily oxidized, temperature and residence time ranges of 250–350 °C and 50–250 s, respectively, were selected. For methanol and acetic acid, since they were more persistent compounds, temperature and residence time ranged from 400 to 500 °C and 10–60 s, respectively. The choice of these temperature and pressure domains allowed the transformation of 10–90% of the organic matter that was required for kinetic studies.

## 3. Results

# 3.1. Pseudo-first-order kinetics

Experiments were carried out assuming a zero order for oxygen concentration since oxygen excess was of one order



Fig. 1. Schematic diagram of the continuous flow reactor system.

of magnitude regarding stoichiometry of the oxidation reaction. The continuous flow reactor was in steady state. Thus, the global kinetic equation could be expressed as follows:

$$-\frac{d\left[\text{COD}\right]}{d\tau} = k\left[\text{COD}\right] \tag{1}$$

where [COD] was the chemical oxygen demand  $(mol l^{-1})$ ,  $\tau$  the residence time in s, and k the reaction rate coefficient  $(s^{-1})$  assuming an Arrhenius law:

$$k = A \, \exp\left(-\frac{E_{\rm a}}{RT}\right) \tag{2}$$

where A was the pre-exponential factor (s<sup>-1</sup>),  $E_a$  the activation energy (J mol<sup>-1</sup>), R the universal gas constant (8.314 J mol<sup>-1</sup> K<sup>-1</sup>), and T the temperature (K).

In expression (1), COD concentration was used instead of the organic molecule concentration. Indeed, COD concentration was chosen as a parameter to describe the global kinetics of the organic compound transformation into  $CO_2$  and  $H_2O$ . Moreover, this approach avoided taking into account the formation of intermediate organic compounds.

Integration of Eq. (1) on the residence times of the organic compounds in the reactor led to the following equation:

$$-\ln\frac{[\text{COD}]}{[\text{COD}]_0} = k\tau \tag{3}$$

where  $[COD]_0$  was the initial chemical oxygen demand  $(mol l^{-1})$ , [COD] the chemical oxygen demand  $(mol l^{-1})$  at  $\tau$ , and *k* the reaction rate coefficient (s<sup>-1</sup>).

The residence time was calculated by addition of the mass flow rates of oxygen and liquid on the basis of the thermodynamic data of oxygen [13] and pure water [14]. The concentration of organic compounds lower than  $5 \text{ g } 1^{-1}$  justified this last assumption. For each temperature, *k* was obtained by a linear regression on experimental [COD] values and residence times, according to Eq. (2). For these experiments, the ratio [COD]/[COD]\_0 varied from 11 to 88%. Fig. 2 shows the Arrhenius plot for the different *k* values obtained at the different temperatures for the hydrothermal oxidation experiments on acetic acid, phenol and methanol. Arrhenius parameters (pre-exponential factor and activation energy) were calculated using a linear regression. Results are reported in Table 1.

#### 3.2. Multiple linear regressions

A set of experiments was performed in order to calculate the oxygen order in the hydrothermal oxidation reaction. The experimental data were analyzed using a multi linear regression method. The continuous flow reactor was in steady state, so that the global rate of transformation of organic compounds in  $CO_2$  by hydrothermal oxidation could be expressed as follows:

rate = 
$$-\frac{d[\text{COD}]}{d\tau} = A \exp\left(-\frac{E_a}{RT}\right) [\text{COD}]^a [\text{O}_2]^b [\text{H}_2\text{O}]^c$$
(4)



Fig. 2. Arrhenius plot for the *k* values calculated by pseudo-first-order kinetics from experimental data obtained at different temperatures for the oxidation of acetic acid, phenol and methanol under oxygen excess. *k* values are means  $\pm 10\%$  and resulted of four different resident times determined at a constant temperature.

where *a*, *b*, and *c* were the reaction orders of organic matter, oxygen, and water, respectively. The reaction rate coefficient was expressed in the Arrhenius form, where *A* was the preexponential factor  $((mol 1^{-1})^{1-a-b-c} s^{-1})$ , and  $E_a$  the activation energy  $(J mol^{-1})$ . For similar reasons as previously mentioned, COD concentration was preferred to organic molecule concentration. As already published, the reaction order of organic compounds in HOT could be assumed equal to unity [9]. Besides, in a reaction medium containing more than 90% of water, the reaction order of water could be considered equal to zero. On these bases, Eq. (4) was simplified to the following one:

rate = 
$$-\frac{d[\text{COD}]}{d\tau} = A \exp\left(-\frac{E_a}{RT}\right) [\text{COD}] [O_2]^b$$
 (5)

In order to treat Eq. (5) with the multiple linear regression analysis, the following steps were applied:

- (1) Experiments were performed in order to get data characterized by the same oxygen stoichiometry (Figs. 3–5).
- (2) For each group and at each temperature, the evolution of COD concentration had to be plotted versus residence time. In all cases, accurate results were obtained using an exponential regression as follows:

$$[\text{COD}] = [\text{COD}]_0 \,\mathrm{e}^{-m\tau} \tag{6}$$

where *m* was the fitting parameter and  $\tau$  the residence time (s). Figs. 3–5 show the results obtained for the three model compounds studied.

(3) The derivation of Eq. (6) allowed to calculate the global reaction rate for the same residence time, for each compound:

$$-\frac{\mathrm{d}\left[\mathrm{COD}\right]}{\mathrm{d}\tau} = [\mathrm{COD}]_0 m \mathrm{e}^{-m\tau} \tag{7}$$

Since all experiments were carried out at a constant  $[COD]_0$ and since [COD] was calculated for the same  $\tau$ , it was possible

Table 1
Kinetic parameters obtained in this work and published in literature

Model compound	$A ((\text{mol } l^{-1})^{1-a-b-c} s^{-1})$	$E_{\rm a}$ (kJ mol <sup>-1</sup> )	$r^2$	а	b	с	$T(^{\circ}C)$	P (MPa)	Conversion rate <sup>a</sup> (mol s <sup><math>-1</math></sup> )	Reference
Acetic Acid										
Pseudo-first-order	$(1.5 \pm 0.2) \times 10^9$	$149 \pm 20$	0.99	1	0	0	400-500	25	$8.1 \times 10^{-3}$	This work
	10 <sup>11.1</sup>	183		1	0	0	425-600	24.6	$1.6 \times 10^{-3}$	[17]
	$2.55 \times 10^{11}$	172.7		1	0	0	338-445	39.4-43.8	$1.8  imes 10^{-2}$	[18]
Multi-linear regression	$(7.6 \pm 0.5) \times 10^{6}$	$115\pm 6$	0.98	1	$0.43\pm0.10$	0	400–500	25	$7.7 \times 10^{-3}$	This work
	$7.84 \times 10^{9}$	168		0.72	0.27	0	425-600	24.6	$1.4 \times 10^{-3}$	[17]
	$4.4 \times 10^{11}$	182		1	0.3	0	420-470	24	$4.8 \times 10^{-3}$	[19]
Runge–Kutta algorithm	$(3.7 \pm 0.4) \times 10^{6}$	$111\pm10$	0.99	1	$0.39\pm0.03$	0	400–500	25	$7.5 \times 10^{-3}$	This work
Methanol										
Pseudo-first-order	$(6.7 \pm 1.2) \times 10^{12}$	$203\pm30$	0.99	1	0	0	400-500	25	$4.5 \times 10^{-3}$	This work
	10 <sup>11.8</sup>	178		1	0	0	400-500	25.3	$1.4  imes 10^{-2}$	[20]
Multi-linear regression	$(4.7 \pm 0.4) \times 10^7$	$125\pm8$	0.96	1	$0.31\pm0.16$	0	400–500	25	$1.1 \times 10^{-2}$	This work
Runge–Kutta algorithm	$(2.4 \pm 0.4) \times 10^{11}$	$175\pm29$	0.99	1	$0.40\pm0.02$	0	400–500	25	$1.2 \times 10^{-2}$	This work
Phenol										
Pseudo-first-order	$(4.2 \pm 1.1) \times 10^3$	$80 \pm 30$	0.94	1	0	0	250-350	25	$3.7 \times 10^{-3}$	This work
Multi-linear regression	$22 \pm 7$	$36\pm3$	0.95	1	$0.24\pm0.06$	0	250-350	25	$2.8 \times 10^{-3}$	This work
	$2.61 \times 10^{5}$	63.8		1	1	0	284-429	29.2-34	$6.7 \times 10^{-3}$	[18]
	10 <sup>1.34</sup>	39.2		1	0	0	300-500	25	$2.6  imes 10^{-4}$	[8]
Runge-Kutta algorithm	$(7.5 \pm 1.7) \times 10^5$	$85\pm14$	0.97	1	$0.24\pm0.05$	0	250-350	25	$3.3 \times 10^{-3}$	This work

*a*, *b*, and *c* are the reaction orders of organic, oxygen, and water, respectively. *T* and *P* are temperature and pressure, respectively. The reaction rate coefficient (*k*) is expressed in Arrhenius form, where *A* is the pre-exponential factor  $((mol l^{-1})^{1-a-b-c} s^{-1})$  and *E*<sub>a</sub> is the activation energy (J mol<sup>-1</sup>), and *r* is the regression coefficient.

<sup>a</sup> Where the conversion rates are calculated from Eq. (4) with:  $[COD]_0 = 0.3125 \text{ mol } l^{-1}$  or  $[CH_3COOH] = 0.156 \text{ mol } l^{-1}$ ;  $[CH_3OH] = 0.208 \text{ mol } l^{-1}$ ;  $[C_6H_5OH] = 0.045 \text{ mol } l^{-1}$ ;  $[O_2]_0 = 0.375 \text{ mol } l^{-1}$ ; temperature of  $450 \degree C$  for acetic acid and methanol, and  $300 \degree C$  for phenol.

to express the reaction rate as

rate = 
$$-\frac{d[\text{COD}]}{d\tau} = A^* \exp\left(-\frac{E_a}{RT}\right) [O_2]^b$$
 (8)

where  $A^* = A$  [COD] = A [COD]<sub>0</sub> e<sup>-m\tau</sup> was a constant value.

$$\ln\left(-\frac{d\left[\text{COD}\right]}{d\tau}\right) = \log A^* - \frac{E_a}{R}\frac{1}{T} + b\log\left[\text{O}_2\right]$$
(9)

Finally, Eq. (8) could be expressed as a linear equation. Starting from the [COD] decreasing rate and the oxygen concentration, the characteristic parameters  $E_a$ , A and b were determined by the multiple linear regression of Eq. (9). Results obtained for the three model compounds are reported in Table 1.

#### 3.3. Runge–Kutta algorithm

When analyzing the experimental data using the Runge–Kutta algorithm, the oxygen concentration at any time was expressed as a function of the initial oxygen concentration and the final COD concentration. The oxygen in the reaction medium could be expressed as follows:

$$[O_2] = ([O_2]_0 - ([COD]_0 - [COD]))$$
(10)

According to Eq. (5), the global reaction rate was deduced:

rate = 
$$-\frac{d [COD]}{d\tau}$$
  
=  $k [COD]^1 ([O_2]_0 - ([COD]_0 - [COD]))^b$  (11)

where  $[COD]_0$  and  $[O_2]_0$  corresponded to  $\tau = 0$ ; k was the global kinetic constant regarding COD disappearance.

This differential equation was solved numerically by a method using the Runge–Kutta algorithm managed by a Fortran program. In this algorithm, the integration interval from 0 to the global residence time ( $\tau_N$ ) was divided into *N* subintervals with  $h = \tau_n/N$ . The set of equations used in this method was reported hereafter:

$$\begin{cases} k_1 = f(\tau_n, \text{COD}_n) \\ k_2 = f(\tau_n + \frac{h}{2}, \text{COD}_n + h\frac{k_1}{2}) \\ k_3 = f(\tau_n + \frac{h}{2}, \text{COD}_n + h\frac{k_2}{2}) \\ k_4 = f(\tau_n + h, \text{COD}_n + hk_3) \\ \text{COD}_{n+1} = \text{COD}_n + \frac{h}{6}(k_1 + 2k_2 + 2k_3 + k_4) \end{cases}$$

$$n = 0, \dots, N - 1$$

where  $\tau_n = n h$ ,  $k_1$ ,  $k_2$ ,  $k_3$ ,  $k_4$  were the internal parameters defined in the Runge–Kutta algorithm; [COD]<sub>n</sub> and [COD]<sub>n+1</sub> were the calculated COD concentrations at  $\tau_n$  and  $\tau_{n+1}$ , respectively. k and b values were fixed starting values from



Fig. 3. Evolution of COD vs. residence time at different temperatures for experiments of acetic acid oxidation with different amounts of oxygen. COD values are means  $\pm 10\%$  of two independent experiments.



Fig. 4. Evolution of COD vs. residence time at different temperatures for experiments of methanol oxidation with different amounts of oxygen. COD values are means  $\pm 10\%$  of two independent experiments.



Fig. 5. Evolution of COD vs. residence time at different temperatures for experiments of phenol oxidation with different amounts of oxygen. COD values are means  $\pm 10\%$  of two independent experiments.

literature for the first run of algorithm.  $[COD]_N$ , that corresponded to the COD concentration calculated for global residence time, was obtained for all experiments performed on the model molecules at one temperature. At least 13 experiments were carried out on each model molecule, for each temperature. These  $[COD]_N$  were compared to the final experimental COD concentrations ( $[COD]_{exp}$ ) and an adjustment of both *k* and *b* values were performed in order to get the best fitting between the calculated  $[COD]_N$  and experimental ones. Starting from the calculated values of *k* at different temperatures, activation energy of the three chemical reactions were determined by linear regression in an Arrhenius plot. Fig. 6 and Table 1 present the results obtained.

# 4. Discussion

First, it was worth noting that the power-law rate expressions were equations that only reflected the general trend of the experimental data. They did not describe in detail the complex oxidation reaction. The way to better understand and control the oxidation reaction goes through the knowledge of the kinetic model, consisting of elementary reaction steps. This was not the main goal of this work that focused on the validation of simple methods for experimental data analysis in order to get real waste kinetic parameters for the scale-up of hydrothermal oxidation units. As already mentioned, the global reaction orders published in the literature were only relevant of the reaction conditions used in the kinetic study. Experimental factors such as the geometry of the injection port that allows the mixing of the organic matter and the oxygen, affected the global kinetic parameters obtained [15]. Indeed, one of the assumptions of power-law rate expressions was an instantaneous mixing of wastewaters with oxygen. Some simulations have clearly shown that this was



Fig. 6. Arrhenius plot for the k values calculated by Runge–Kutta algorithm from experimental data obtained at different temperatures for the oxidation of acetic acid, phenol and methanol. For each organic compound, k values are means of the experimental data reported in Figs. 3–5, at a constant temperature.

not the case [16]. Although the activation energy was not an intrinsic parameter, it could be considered as a parameter that predicts the temperature dependence upon the COD disappearance rate in the operating conditions of the study. Thus, this kinetic parameter can be used for the scale-up of industrial units which are developed with the same concept and flowsheet as the pilot plant facility.

Data obtained with experimental conditions similar to those used in this work could be accurately compared. Thus, only studies using the following characteristics were considered: (i) non catalytic hydrothermal oxidation; (ii) plug flow reactor (without packed bed); (iii) pressure close to 25 MPa; (iv) temperature ranges between 250 and 350 °C for phenol and 400 and 500 °C for acetic acid and methanol; (v) pure oxygen as oxidant. Moreover, besides the simple comparison of the Arrhenius parameters (*A* and  $E_a$ ) reported in Table 1, for acetic acid [17–19], methanol [20] and phenol [18,8], the reaction orders of organic, oxygen and water were also reported in Table 1. This implied the choice of a same fixed set of operating conditions that were defined hereafter:

- $[COD]_0 = 0.3125 \text{ mol } l^{-1}$  or  $[CH_3COOH] = 0.156 \text{ mol } l^{-1}; [CH_3OH] = 0.208 \text{ mol } l^{-1};$  $[C_6H_5OH] = 0.045 \text{ mol } l^{-1}.$
- 20% oxygen excess from stoichiometry, so  $[O_2]_0 = 0.375 \text{ mol } 1^{-1}$ .
- Temperature of 450 °C for acetic acid and methanol, and 300 °C for phenol.

Kinetic parameters for pseudo-first-order kinetics, obtained with an oxygen excess of one order of magnitude regarding stoichiometry of the oxidation reaction, were in good agreement with those previously published in the literature taking into account the accuracy of our results. It is important to point out that the assumption of hydrothermal oxidation reaction assuming a zero order for oxygen concentration limited drastically the application of the kinetic equation in the simulation of industrial HOT process. The pseudo-first-order kinetics did not consider a decrease in the kinetic reaction rate when the oxygen concentration decreased significantly in the reactor. It is obvious that an industrial HOT process cannot operate with great oxygen excess, so a kinetic equation that takes into account the effect of oxygen concentration is needed. In this way, experiments were performed in order to calculate the oxygen order in the hydrothermal oxidation reaction. At first, the experimental data were treated by multiple linear regressions as classically used. The kinetic results obtained (Table 1) for acetic acid were close to those previously published. Same agreement was obtained for the kinetic results for phenol (Table 1) and literature data in the same temperature range. In contrast, when the temperature range between 300 and 500 °C was considered, the kinetic results were different of one order of magnitude. This result remained unexplained.

The kinetic results obtained by linear regression, when the oxygen content was lower and higher than the stoichiometry, were in good agreement with those obtained by pseudo-firstorder kinetics, with an oxygen excess of one order of magnitude regarding stoichiometry of the oxidation reaction. This validated that the rates determining steps of oxidation reaction were similar when the oxygen content varied from 0.4 to 1.4, regarding the stoichiometry.

The use of multiple linear regressions implied to carry out a set of experiments with the same amount of oxygen at any residence time. This implied to collect numerous experimental data that might be difficult to obtain. Generally, three or four experimental data were used for the kinetic parameter determination. In this way, Runge-Kutta algorithm was used for fitting together all experimental data. The kinetic results obtained (Table 1) for acetic acid, methanol and phenol were close to those obtained in this study with the two other kinetic parameter determination method. We can consider that Runge-Kutta algorithm was validated for experimental data treatment in order to get global kinetic parameters. This algorithm was a more efficient calculation method for this kind of analysis, because the use of this method allowed simplifying the set-up of experiments by suppression of experiments with the same amount of oxygen at any residence time.

# 5. Conclusion

The main goal of this work was to validate Runge-Kutta algorithm for experimental data analysis in order to get, in a simplest way, the real waste kinetic parameters for the scaleup of hydrothermal oxydation units. At first, global kinetic parameter was determined with pseudo-first-order kinetics assuming a zero-order for oxygen concentration. At second, oxygen order for oxygen concentration on the rate of organic compound oxidation was determined by multiple linear regressions. Based on these two methods of experimental data analysis, Runge-Kutta algorithm was validated for the determination of kinetic parameters starting from experimental data. The main advantages of Runge-Kutta algorithm for experimental data treatments, regarding multi-linear regression method, were: (i) the possibility of fitting together all experimental data obtained at the same temperature; (ii) the suppression of experiments with the same amount of oxygen at any residence time. Runge-Kutta algorithm could be used for the determination of kinetic parameters of real wastewaters starting from experimental data obtained by the ICMCB pilot scale laboratory and on the two industrial pilot plant facilities developed by HOO company [21]. These pilots were based on a new concept of HOT reactor [22] and a capacity of 100 kg/h of waste treatment capacity.

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